

Codes and Ciphers	UNIT 16 <i>Modern Encryption</i> Lesson Plan 1	<i>Encryption</i>																																
Activity 1	<p>Introduction</p> <p>T: With the advent of powerful and cheap computers, software allows us to encrypt quickly and easily. Here is an example, called</p> <div style="border: 1px solid black; padding: 2px; display: inline-block;">Rijndael</div> also known as <div style="border: 1px solid black; padding: 2px; display: inline-block;">Advanced Encryption Standard (AES)</div> This is often used for internet security. We'll go through the method together; it has four steps: <div style="border: 1px solid black; padding: 5px; margin: 5px 0;"> <ul style="list-style-type: none"> • substitution (we'll use a Caesar substitution) • row shift • column transformation • add key </div> <p>T: It looks complex although it is really straightforward, but much quicker for a computer than for us!</p> <p style="text-align: right;"><i>5 mins</i></p>	<p style="text-align: center;">Notes</p> <p>T: Teacher P: Pupil Ex.B: Exercise Book</p> <p>Discussion about security and, in particular, internet security used for international companies. T should find out if Ps have any direct knowledge of systems, and build on their experiences.</p> <p>T writes the information on the board.</p>																																
2	<p>Caesar substitution</p> <p>T: We start with a plaintext message</p> <div style="border: 1px solid black; padding: 2px; display: inline-block; margin: 5px 0;">HI HERE IS A MESSAGE</div> <p>T: How many letters in this message? <i>(16)</i></p> <p>T: We can put this in a 4×4 grid, writing the message down the columns. Who would like to do this?</p> <p>P₁ (on board):</p> <table border="1" style="border-collapse: collapse; text-align: center; margin: 5px 0;"> <tr><td>H</td><td>R</td><td>A</td><td>S</td></tr> <tr><td>I</td><td>E</td><td>M</td><td>A</td></tr> <tr><td>H</td><td>I</td><td>E</td><td>G</td></tr> <tr><td>E</td><td>S</td><td>S</td><td>E</td></tr> </table> <p>T: Look at your copy of the Caesar substitution we are going to use. What is the shift? <i>(By 3)</i></p> <p>T: What else do you notice? <i>(Some punctuation marks are included as well as letters)</i></p> <p>T: What does the message now become?</p> <p>P₂ (on board):</p> <table border="1" style="border-collapse: collapse; text-align: center; margin: 5px 0;"> <tr><td>K</td><td>U</td><td>D</td><td>V</td></tr> <tr><td>L</td><td>H</td><td>P</td><td>D</td></tr> <tr><td>K</td><td>L</td><td>H</td><td>J</td></tr> <tr><td>H</td><td>V</td><td>V</td><td>H</td></tr> </table> <p>T: Now encrypt</p> <div style="border: 1px solid black; padding: 2px; display: inline-block; margin: 5px 0;">OUR SECRET MESSAGE</div> in the same way. <p style="text-align: right;"><i>15 mins</i></p>	H	R	A	S	I	E	M	A	H	I	E	G	E	S	S	E	K	U	D	V	L	H	P	D	K	L	H	J	H	V	V	H	<p>Ps should be familiar with this concept but might need reminding of the technique.</p> <p>This part of the lesson should be as interactive as possible, with Ps working at the board.</p> <p>OS 16.1 should be shown or a grid drawn on the board.</p> <p>A copy of OS 16.2 is given to each P.</p> <p>Volunteer P at board.</p> <p>T gives Ps a few minutes to complete this. They could use a copy of OS 16.1. Interactive review of answers; T must ensure that all Ps have understood.</p>
H	R	A	S																															
I	E	M	A																															
H	I	E	G																															
E	S	S	E																															
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<p>Activity</p> <p>3</p>	<p>Row shift</p> <p>T: The next step involves shifting the rows of the grid:</p> <p style="padding-left: 40px;">first row – no shift second row – shift left by 1 third row – shift left by 2 fourth row – shift left by 3</p> <p>We can show this by</p> <table border="1" style="margin-left: 40px;"> <tr><td> </td><td> </td><td> </td><td> </td></tr> <tr><td> </td><td> </td><td>←</td><td> </td></tr> <tr><td> </td><td>←</td><td>←</td><td> </td></tr> <tr><td>←</td><td> </td><td> </td><td> </td></tr> </table> <p>What does our message become?</p> <p>P₃ (on board):</p> <table border="1" style="margin-left: 40px;"> <tr><td>K</td><td>U</td><td>D</td><td>V</td></tr> <tr><td>H</td><td>P</td><td>D</td><td>L</td></tr> <tr><td>H</td><td>J</td><td>K</td><td>L</td></tr> <tr><td>H</td><td>H</td><td>V</td><td>V</td></tr> </table> <p>T: Now it's your turn; continue with your example.</p> <p style="text-align: right;">20 mins</p>							←			←	←		←				K	U	D	V	H	P	D	L	H	J	K	L	H	H	V	V	<p>Notes</p> <p>Interactive introduction with T making sure that Ps understand the concepts.</p> <p>T chooses a P (or volunteer) to work at the board; other Ps help if there is confusion.</p> <p>Ps have a few minutes for this; T monitors progress. Review, with T sorting out any misconceptions.</p>
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	←	←																																
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K	U	D	V																															
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H	J	K	L																															
H	H	V	V																															
<p>4</p> <p><i>(continued)</i></p>	<p>Column transformation</p> <p>T: Here we make a transformation; for each column –</p> <table border="1" style="margin-left: 40px;"> <tr><td>A</td><td>B+C+D</td></tr> <tr><td>B</td><td>A+C+D</td></tr> <tr><td>C</td><td>A+B+D</td></tr> <tr><td>D</td><td>A+B+C</td></tr> </table> <p>and for this to make sense, we add letters by putting them into binary.</p> <p>T: Look at your copy of the binary code. Are all possible codes used? <i>(Yes, all 32)</i></p> <p>T: For addition, we use the rules</p> <table border="1" style="margin-left: 40px;"> <tr><td>0 + 0 = 1</td><td>0 + 1 = 1</td></tr> <tr><td>1 + 0 = 1</td><td>1 + 1 = 0</td></tr> </table> <p><i>(This is called 'exclusive OR-ing' and is extensively used in computing)</i></p> <p>T: How can we write H + H ? <i>(01000 + 01000)</i></p> <p>T: Good. Now add the corresponding binary digits. <i>(00000)</i></p> <p>T: What about H + H + H ? <i>(00000 + 01000)</i></p> <p>T: And what is that? <i>(01000)</i></p> <p>T: In letters? <i>(H)</i></p> <p>T: Now try K + H + H.</p> <p>P₁ (on board):</p> $ \begin{aligned} K + H + H &= 01011 + (01000 + 01000) \\ &= 01011 + 00000 \\ &= 01011 \quad (K) \end{aligned} $	A	B+C+D	B	A+C+D	C	A+B+D	D	A+B+C	0 + 0 = 1	0 + 1 = 1	1 + 0 = 1	1 + 1 = 0	<p>This is more difficult – the explanation is straightforward but it is easy to make errors in the actual calculations.</p> <p>Each P has a copy of OS 16.2.</p> <p>It is important that Ps appreciate these rules and can use them without problems. OS 16.4 can be used by T or each P can be given a copy.</p> <p>This is not easy to explain unless Ps are very flexible and able; T might need to go through several examples or use OS 16.1 where letters are converted to their binary codes – there is no need to go back to letters at the end of this step.</p> <p>The 'sums' can be done in any order; e.g.</p> $ \begin{aligned} &(01011 + 01000) + 01000 \\ &= 00011 + 01000 \\ &= 01011 \end{aligned} $																				
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<p><i>Codes and Ciphers</i></p>	<p>UNIT 16 <i>Modern Encryption</i> Lesson Plan 2</p>	<p><i>Decryption</i></p>																																																																																								
<p>Activity 1</p>	<p>Step 1: Key</p> <p>T: Here we have our received message, in groups of 4 characters.</p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> ' F R A W Y H B , T C , B L U O </div> <p>To decrypt the message, we simply work backwards through the 4 steps, reversing them.</p> <p>T: What do we do first? <i>(Put in the 4 × 4 grid)</i></p> <p>P₁ (at board):</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td>'</td><td>W</td><td>,</td><td>B</td></tr> <tr><td>F</td><td>Y</td><td>T</td><td>L</td></tr> <tr><td>R</td><td>H</td><td>C</td><td>U</td></tr> <tr><td>A</td><td>B</td><td>,</td><td>O</td></tr> </table> <p>T: Well done; what next? <i>(Subtract the key)</i></p> <p>T: Yes – but this is the same as ... what? <i>(Adding)</i></p> <p>T: OK. Who will start this off?</p> <p>P₂: What is the key?</p> <p>T: OURTOPSECRETKEYX ; what is the sum?</p> <p>P₃:</p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td style="border: 1px solid black; padding: 2px;">'</td><td style="border: 1px solid black; padding: 2px;">W</td><td style="border: 1px solid black; padding: 2px;">,</td><td style="border: 1px solid black; padding: 2px;">B</td> <td style="padding: 0 10px;">+</td> <td style="border: 1px solid black; padding: 2px;">O</td><td style="border: 1px solid black; padding: 2px;">O</td><td style="border: 1px solid black; padding: 2px;">C</td><td style="border: 1px solid black; padding: 2px;">K</td> <td style="padding: 0 10px;">=</td> <td style="border: 1px solid black; width: 20px; height: 20px;"></td><td style="border: 1px solid black; width: 20px; height: 20px;"></td><td style="border: 1px solid black; width: 20px; height: 20px;"></td><td style="border: 1px solid black; width: 20px; height: 20px;"></td> </tr> <tr> <td style="border: 1px solid black; padding: 2px;">F</td><td style="border: 1px solid black; padding: 2px;">Y</td><td style="border: 1px solid black; padding: 2px;">T</td><td style="border: 1px solid black; padding: 2px;">L</td> <td></td> <td style="border: 1px solid black; padding: 2px;">U</td><td style="border: 1px solid black; padding: 2px;">P</td><td style="border: 1px solid black; padding: 2px;">R</td><td style="border: 1px solid black; padding: 2px;">E</td> <td></td> <td style="border: 1px solid black; width: 20px; height: 20px;"></td><td style="border: 1px solid black; width: 20px; height: 20px;"></td><td style="border: 1px solid black; width: 20px; height: 20px;"></td><td style="border: 1px solid black; width: 20px; height: 20px;"></td> </tr> <tr> <td style="border: 1px solid black; padding: 2px;">R</td><td style="border: 1px solid black; padding: 2px;">H</td><td style="border: 1px solid black; padding: 2px;">C</td><td style="border: 1px solid black; padding: 2px;">U</td> <td></td> <td style="border: 1px solid black; padding: 2px;">R</td><td style="border: 1px solid black; padding: 2px;">S</td><td style="border: 1px solid black; padding: 2px;">E</td><td style="border: 1px solid black; padding: 2px;">Y</td> <td></td> <td style="border: 1px solid black; width: 20px; height: 20px;"></td><td style="border: 1px solid black; width: 20px; height: 20px;"></td><td style="border: 1px solid black; width: 20px; height: 20px;"></td><td style="border: 1px solid black; width: 20px; height: 20px;"></td> </tr> <tr> <td style="border: 1px solid black; padding: 2px;">A</td><td style="border: 1px solid black; padding: 2px;">B</td><td style="border: 1px solid black; padding: 2px;">,</td><td style="border: 1px solid black; padding: 2px;">O</td> <td></td> <td style="border: 1px solid black; padding: 2px;">T</td><td style="border: 1px solid black; padding: 2px;">E</td><td style="border: 1px solid black; padding: 2px;">T</td><td style="border: 1px solid black; padding: 2px;">X</td> <td></td> <td style="border: 1px solid black; width: 20px; height: 20px;"></td><td style="border: 1px solid black; width: 20px; height: 20px;"></td><td style="border: 1px solid black; width: 20px; height: 20px;"></td><td style="border: 1px solid black; width: 20px; height: 20px;"></td> </tr> </table> <p>T: Each of you can do one sum and put in your answer.</p> <p>Ps:</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td>Q</td><td>X</td><td>X</td><td>I</td></tr> <tr><td>S</td><td>I</td><td>F</td><td>I</td></tr> <tr><td>-</td><td>,</td><td>F</td><td>L</td></tr> <tr><td>U</td><td>G</td><td>O</td><td>W</td></tr> </table> <p style="text-align: right;"><i>15 mins</i></p>	'	W	,	B	F	Y	T	L	R	H	C	U	A	B	,	O	'	W	,	B	+	O	O	C	K	=					F	Y	T	L		U	P	R	E						R	H	C	U		R	S	E	Y						A	B	,	O		T	E	T	X						Q	X	X	I	S	I	F	I	-	,	F	L	U	G	O	W	<p style="text-align: center;"><i>Notes</i></p> <p>T can use either the received message from the encryption example in Lesson Plan 1, or this new message.</p> <p>T might need to justify the methods but it is sometimes enough just to see the method working.</p> <p>This stage might need more explanation. As with the encryption, T can work with the binary representation, using OS 16.4.</p> <p>Assign one sum to each P; use other Ps to check the work, in pairs, etc. T should check each answer as it is presented.</p>
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<p>2</p> <p><i>(continued)</i></p>	<p>Step 2: column transformation</p> <p>T: As with the key, the column transformation is also 'self inverse' – to reverse it, we do the same thing again!</p> <p>T: What happens to the first column?</p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td style="border: 1px solid black; padding: 2px;">Q</td> <td style="padding: 0 10px;">→</td> <td style="border: 1px solid black; padding: 2px;">S</td><td style="border: 1px solid black; padding: 2px;">+</td><td style="border: 1px solid black; padding: 2px;">-</td><td style="border: 1px solid black; padding: 2px;">+</td><td style="border: 1px solid black; padding: 2px;">U</td> </tr> <tr> <td style="border: 1px solid black; padding: 2px;">S</td> <td></td> <td style="border: 1px solid black; width: 20px; height: 20px;"></td><td style="border: 1px solid black; width: 20px; height: 20px;"></td><td style="border: 1px solid black; width: 20px; height: 20px;"></td><td style="border: 1px solid black; width: 20px; height: 20px;"></td><td style="border: 1px solid black; width: 20px; height: 20px;"></td> </tr> <tr> <td style="border: 1px solid black; padding: 2px;">-</td> <td></td> <td style="border: 1px solid black; width: 20px; height: 20px;"></td><td style="border: 1px solid black; width: 20px; height: 20px;"></td><td style="border: 1px solid black; width: 20px; height: 20px;"></td><td style="border: 1px solid black; width: 20px; height: 20px;"></td><td style="border: 1px solid black; width: 20px; height: 20px;"></td> </tr> <tr> <td style="border: 1px solid black; padding: 2px;">U</td> <td></td> <td style="border: 1px solid black; width: 20px; height: 20px;"></td><td style="border: 1px solid black; width: 20px; height: 20px;"></td><td style="border: 1px solid black; width: 20px; height: 20px;"></td><td style="border: 1px solid black; width: 20px; height: 20px;"></td><td style="border: 1px solid black; width: 20px; height: 20px;"></td> </tr> </table> <p>Who can complete the next three rows?</p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td style="border: 1px solid black; padding: 2px;">Q</td> <td style="padding: 0 10px;">→</td> <td style="border: 1px solid black; padding: 2px;">S</td><td style="border: 1px solid black; padding: 2px;">+</td><td style="border: 1px solid black; padding: 2px;">-</td><td style="border: 1px solid black; padding: 2px;">+</td><td style="border: 1px solid black; padding: 2px;">U</td> </tr> <tr> <td style="border: 1px solid black; padding: 2px;">S</td> <td></td> <td style="border: 1px solid black; padding: 2px;">Q</td><td style="border: 1px solid black; padding: 2px;">+</td><td style="border: 1px solid black; padding: 2px;">-</td><td style="border: 1px solid black; padding: 2px;">+</td><td style="border: 1px solid black; padding: 2px;">U</td> </tr> <tr> <td style="border: 1px solid black; padding: 2px;">-</td> <td></td> <td style="border: 1px solid black; padding: 2px;">Q</td><td style="border: 1px solid black; padding: 2px;">+</td><td style="border: 1px solid black; padding: 2px;">S</td><td style="border: 1px solid black; padding: 2px;">+</td><td style="border: 1px solid black; padding: 2px;">U</td> </tr> <tr> <td style="border: 1px solid black; padding: 2px;">U</td> <td></td> <td style="border: 1px solid black; padding: 2px;">Q</td><td style="border: 1px solid black; padding: 2px;">+</td><td style="border: 1px solid black; padding: 2px;">S</td><td style="border: 1px solid black; padding: 2px;">+</td><td style="border: 1px solid black; padding: 2px;">-</td> </tr> </table> <p>T: Good. And the next stage? <i>(Work out these sums)</i></p> <p style="text-align: center;">etc.</p>	Q	→	S	+	-	+	U	S							-							U							Q	→	S	+	-	+	U	S		Q	+	-	+	U	-		Q	+	S	+	U	U		Q	+	S	+	-	<p>The first part might need more explanation; it works because the 'addition' values are also self inverse.</p> <p>As with encryption, T can either use the binary representations (and use OS 16.4) or use the letters and binary as in the plan.</p>																																
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<p>Activity</p> <p>2 (continued)</p>	<p> $P_1: S+_+U \Rightarrow 10011 + 00000 + 10101$ $= 00110 \Rightarrow F$ </p> <p> $P_2: Q+_+U \Rightarrow 10001 + 00000 + 10101$ $= 00100 \Rightarrow D, \text{ etc.}$ </p> <p>T: Now complete the other column transformations.</p> <p>T: This is the new message:</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td>F</td><td>U</td><td>O</td><td>R</td></tr> <tr><td>P</td><td>D</td><td>Q</td><td>R</td></tr> <tr><td>W</td><td>V</td><td>Q</td><td>W</td></tr> <tr><td>B</td><td>J</td><td>X</td><td>L</td></tr> </table> <p style="text-align: right;">30 mins</p>	F	U	O	R	P	D	Q	R	W	V	Q	W	B	J	X	L	<p style="text-align: center;">Notes</p> <p>Ps will need time to complete this. T should monitor progress; then review and correct mistakes. It is very easy to make a mistake!</p>																																				
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<p>3</p>	<p>Step 3: row shift</p> <p>T: How do we do this? <i>(Shift in opposite direction)</i></p> <p>T: Well done! We can summarise this as</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td></td><td></td><td></td><td></td></tr> <tr><td>→</td><td></td><td></td><td></td></tr> <tr><td>→</td><td>→</td><td></td><td></td></tr> <tr><td>→</td><td>→</td><td>→</td><td></td></tr> </table> <p>T: I need three volunteers to do this on the board:</p> <p>Ps:</p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td style="border: 1px solid black; padding: 2px;">F</td><td style="border: 1px solid black; padding: 2px;">U</td><td style="border: 1px solid black; padding: 2px;">O</td><td style="border: 1px solid black; padding: 2px;">R</td> <td style="padding: 0 10px;">→</td> <td style="border: 1px solid black; padding: 2px;">F</td><td style="border: 1px solid black; padding: 2px;">U</td><td style="border: 1px solid black; padding: 2px;">O</td><td style="border: 1px solid black; padding: 2px;">R</td> </tr> <tr> <td style="border: 1px solid black; padding: 2px;">P</td><td style="border: 1px solid black; padding: 2px;">D</td><td style="border: 1px solid black; padding: 2px;">Q</td><td style="border: 1px solid black; padding: 2px;">R</td> <td></td> <td style="border: 1px solid black; padding: 2px;">R</td><td style="border: 1px solid black; padding: 2px;">D</td><td style="border: 1px solid black; padding: 2px;">D</td><td style="border: 1px solid black; padding: 2px;">Q</td> </tr> <tr> <td style="border: 1px solid black; padding: 2px;">W</td><td style="border: 1px solid black; padding: 2px;">V</td><td style="border: 1px solid black; padding: 2px;">Q</td><td style="border: 1px solid black; padding: 2px;">W</td> <td></td> <td style="border: 1px solid black; padding: 2px;">Q</td><td style="border: 1px solid black; padding: 2px;">W</td><td style="border: 1px solid black; padding: 2px;">W</td><td style="border: 1px solid black; padding: 2px;">V</td> </tr> <tr> <td style="border: 1px solid black; padding: 2px;">B</td><td style="border: 1px solid black; padding: 2px;">J</td><td style="border: 1px solid black; padding: 2px;">X</td><td style="border: 1px solid black; padding: 2px;">L</td> <td></td> <td style="border: 1px solid black; padding: 2px;">J</td><td style="border: 1px solid black; padding: 2px;">X</td><td style="border: 1px solid black; padding: 2px;">L</td><td style="border: 1px solid black; padding: 2px;">B</td> </tr> </table> <p style="text-align: right;">35 mins</p>					→				→	→			→	→	→		F	U	O	R	→	F	U	O	R	P	D	Q	R		R	D	D	Q	W	V	Q	W		Q	W	W	V	B	J	X	L		J	X	L	B	<p>Interactive discussion on method, with Ps at board completing the shift. T should ensure that all Ps have understood.</p>
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F	U	O	R	→	F	U	O	R																																														
P	D	Q	R		R	D	D	Q																																														
W	V	Q	W		Q	W	W	V																																														
B	J	X	L		J	X	L	B																																														
<p>4</p>	<p>Step 4: Caesar substitution</p> <p>T: What next? <i>(Reverse the shift of 3 letters)</i></p> <p>T: OK – it's your turn now.</p> <p>T: Who has the message? <i>(CONGRATULATIONS!)</i></p> <p style="text-align: right;">45 mins</p>	<p>Hopefully, Ps will see what to do; T makes sure that they have understood and encourages Ps to work as fast as possible to determine the message. Praise for those who are successful.</p>																																																				
	<p>Homework</p> <p>Decrypt the message</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td>K</td><td>F</td><td>K</td><td>Z</td></tr> <tr><td>Y</td><td>X</td><td>P</td><td>I</td></tr> <tr><td>R</td><td>,</td><td>W</td><td>T</td></tr> <tr><td>,</td><td>N</td><td>I</td><td>N</td></tr> </table> <p>with the original key.</p>	K	F	K	Z	Y	X	P	I	R	,	W	T	,	N	I	N																																					
K	F	K	Z																																																			
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